

D 52791

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Name.....

Reg. No.....

FIRST SEMESTER B.Sc. DEGREE EXAMINATION, NOVEMBER 2018

(CUCBCSS—UG)

Complementary Course (Statistics)

STS 1C 01—BASIC STATISTICS AND PROBABILITY

Time : Three Hours

Maximum : 80 Marks

Section A

Answer all questions in one word.

Each question carries 1 mark.

Fill up the blanks :

1. Let A and B be two events such that  $P(A) = 0.3$  and  $P(A \cup B) = 0.79$ . If A and B are independent events, then  $P(B) =$  \_\_\_\_\_.
2. The type of sampling in which each unit of the population has an equal chance of being included in the sample is called \_\_\_\_\_.
3. Let  $b_1$  and  $b_2$  are the regression coefficients, then the correlation coefficient is \_\_\_\_\_.
4. A coin is tossed three times in succession, the number of sample points in the sample space is \_\_\_\_\_.
5. When all the values are equal, the standard deviation would be \_\_\_\_\_.

Write True or False :

6. Mutually exclusive events are independent.
7. If  $F(x)$  be the cumulative distribution function of a random variable, then  $0 \leq F(x) \leq 1$ .
8. Mean lies between median and mode.
9. In a moderately asymmetrical distribution, the mean, median and mode are the same.
10. Correlation coefficient is independent of change of origin and scale.

(10 × 1 = 10 marks)

Turn over

## Section B

Answer all questions in one sentence each.  
Each question carries 2 marks.

11. Define primary data.
12. Give the normal equations for fitting the straight line  $y = a + bx$ .
13. What do you mean by probability mass function?
14. Define random experiment with an example.
15. How will you compute mode for a frequency distribution?
16. Define Population.
17. How can the two regression lines be identified?

(7 × 2 = 14 marks)

## Section C

Answer any three questions.  
Each question carries 4 marks.

18. The ranks of the same 10 students in two subjects A and B are given below :

(3, 6), (5, 4), (8, 9), (4, 8), (7, 1), (10, 2), (2, 3), (1, 10), (6, 5) and (9, 7). Find the rank correlation coefficient.

19. Fit a straight line of the form  $y = ax + b$  to the following data :

$x$	:	1	3	5	7	8	10
$y$	:	8	12	15	17	18	20

20. Explain the desirable properties of a good average.
21. Prove that for any discrete distribution, standard deviation is not less than mean deviation from the mean.
22. A discrete random variable has the following probability distribution :

$X$	:	0	1	2	3	4	5	6	7	8
$p(x)$	:	$a$	$3a$	$5a$	$7a$	$9a$	$11a$	$13a$	$15a$	$17a$

Find (i) the value of  $a$  ; and (ii)  $P(X < 3)$ .

(3 × 4 = 12 marks)

## Section D

Answer any four questions.  
Each question carries 6 marks.

23. From the following information obtain the correlation coefficient :

$$n = 12, \sum x = 30, \sum y = 5, \sum x^2 = 670, \sum y^2 = 285, \sum xy = 334.$$

24. Define coefficient of variation. Compute the same for the observations 7, 9, 10, 8, 6 and 5.
25. A man travels 600 km. by train at an average speed of 60 km/h. 300 km. by boat at an average speed of 15 km./h, 700 km. by plane at 350 km/h and 25 km. by a taxi at 50 km./h. Find the average speed of the whole journey.

26. If  $p(x) = (0.1)^x$  ;  $x = 1, 2, 3, 4$ . Find (i)  $P[X = 1 \text{ or } 2]$  ; and (ii)  $P\left[\frac{1}{2} < X < \frac{5}{2} \mid X > 1\right]$ .

27. Two random variables X and Y have the following joint probability density function :

$$f(x, y) = \begin{cases} 2 - x - y; & 0 \leq x \leq 1, \quad 0 \leq y \leq 1 \\ 0; & \text{otherwise.} \end{cases}$$

Find (i) marginal density functions of X and Y ; and (ii) conditional density functions.

28. Define pairwise independence and mutual independence of events. Discuss the implication between them.

(4 × 6 = 24 marks)

## Section E

Answer any two questions.  
Each question carries 10 marks.

29. The following table gives the marks obtained by some students. Calculate mean, median and mode :

Marks	:	0-10	10-20	20-30	30-40	40-50
Frequency	:	3	13	18	12	5

30. From the following data of values of X and Y, find the regression equation of Y on X :

X	:	2	3	4	5	6
Y	:	3	5	4	8	9

Turn over

31. (a) Give the axiomatic definition of probability.
- (b) A committee of four has to be formed from among 3 economists, 4 engineers, 2 statisticians and 1 doctor.
- What is the probability that each of the four professions is represented on the committee?
  - What is the probability that the committee consists of the doctor and at least one economist?
32. State Baye's Theorem. A machine part is produced by three factories A, B and C. Their proportion of production is 25, 35 and 40 per cent respectively. Also, the percentage defective manufactured by the three factories are 5, 4 and 3 respectively. A part is taken at random and is found to be defective. Obtain the probability that the selected part belongs to factory B.

(2 × 10 = 20 marks)