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FOURTH SEMESTER B.Sc. DEGREE EXAMINATION, APRIL 2016

(CUCBCSS-UG)

Complementary Course

MAT 4C 04-MATHEMATICS

Time: Three Hours

Maximum: 80 Marks

Part A

Objective type. Answer all twelve questions.

- 1. What do you mean by a non linear differential equation?
- 2. Write the solution for an homogeneous differential equation with $2 \pm 3i$ as a double root for its auxillary equation.
- State the Existence and Uniqueness theorem for initial value problem.
- 4. What is the Shifting property of Laplace transform?
- 5. Find $L^{-1} \left(\frac{1}{(s+1)^2} \right)$.
- What is $L(t^{-1/2})$?
- How do you define a sawtooth wave function?
- Define and give an example of an odd function.
- Write the Euler's formula for a fourier series of a periodic function.
- Write the formula for Runge Kutta method.
- Does the inital value problem xy' = 4y, y(0) = 1 has solution? Give reason.
- Give a formula for an error for Simpson's rule.

 $(12 \times 1 = 12 \text{ marks})$

Part B

Short answer type. Answer any nine questions.

- 13. Find the particular integral for $y'+4y=8x^2$.
- 14. Find a basis for the solution of the differential equation y' y = 0.
- 15. Find $W[e^{\lambda}, xe^{\lambda}]$.

Turn over

- 16. If $L^{-1}(f(s)) = F(t)$ then show that $L^{-1}(f(s-a)) = e^{st} F(t)$.
- 17. Show that the Laplace transform is a linear operation.
- 18. Find L (sin2t).
- 19. Show that the function f(x) = constant is a periodic function of period p for every positive p.
- 20. Find the fourier series of f(x) = -1, $-\pi < x < \pi$.
- 21. Show that $u = \cos 4t \sin 2x$ is a solution of the wave equation.
- 22. Apply Picard's iteration upto 4 steps to solve y' = y and y(0) = 1.
- 23. Show that the initial value problem $y' = \sqrt{|y|}$, y(0) = 0 does not have a unique solution.
- 24. What do you mean by Lipschitz condition?

 $(9 \times 2 = 18 \text{ mark})$

Part C

Short essay.

Answer any six questions.

- 25. Solve $x^2y'' + 7xy' + 13y = 0$.
- 26. Verify $y_p = 2x^2 6x + 7$ is a solution for $y'' + 3y' + 2y = 4x^2$ and find a general solution.
- 27. Find the Laplace transform of $f(t) = \begin{cases} t, 0 < t < 4 \\ 5, t > 4 \end{cases}$.
- 28. Find $L^{-1}\left(\frac{3s+16}{s^2-s-6}\right)$.
- 29. Solve $u_y = 2xyu$.
- 30. Find the cosine series of f(x) = x, 0 < x < L.
- 31. Solve the integral equation $y(t) = t + \int_0^t y(\tau) \sin(t \tau) d\tau$.
- 32. Using Simpson's rule evaluate the integral $\int_{1}^{2} x \, dx$ with n = 4 and hence find an upper bound to the error incurred.
- Apply improved Euler method in 3 steps to solve y' = y, y(0) = 1 with h = 0.1. Also find the effection occurred.

(6 × 5 = 30 marks

Part D

Answer any two questions.

- 34. (a) Solve $x^2y'' 4xy' + 6y = 21x^{-1}$.
 - (b) Solve the initial value problem $(D^2 + 4) y = -12 \sin 2x$, y(0) = 1.8, y'(0) = 5.
- 35. Solve the integral equation $y(t) = t + \int_0^t y(\tau) \sin(t \tau) d\tau$.
- 36. Find the fourier series of $f(x) = \begin{cases} x^2, -\frac{\pi}{2} < x < \frac{\pi}{2} \\ \frac{\pi^2}{4}, \frac{\pi}{2} < x < \frac{3\pi}{2} \end{cases}$.

 $(2 \times 10 = 20 \text{ marks})$