

**FOURTH SEMESTER B.Sc. DEGREE EXAMINATION, APRIL/MAY 2015**

(U.G.-CCSS)

Complementary Course—Mathematics

MM 4C 04—MATHEMATICS

Time : Three Hours

Maximum : 30 Weights

**Unit I**

*Answer all twelve questions.*

1. Which of the following is not a solution of  $y'' - y = 0$ ?
  - (a)  $e^x$ .
  - (b)  $e^{-x}$ .
  - (c)  $e^x + e^{-x}$ .
  - (d)  $1 + e^x$ .
2. Find the general solution of  $y'' + 9y' + 20y = 0$ .
3. Write a pair of basis solutions of  $x^2 y'' - 4xy' + 6y = 0$ .
4. If  $y_1 = e^{2x}$ ,  $y_2 = e^{-x}$  find  $w(y_1, y_2)$ .
5. Find the Laplace transform of  $\sin wt$ .
6. Find  $L^{-1} \left( \frac{60 + 6s^2 + s^4}{s^7} \right)$ .
7.  $f(x) = x^3 + 2x^2$  is an :
  - (a) Even Function.
  - (b) Odd function.
  - (c) Neither even nor odd.
  - (d) Either even or odd.
8. Write the one dimensional wave equation.
9. Find the smallest period  $p$  of  $\cos \pi x$ .
10. Plot the function  $f(x) = x|x|$ ,  $-\pi < x < \pi$ .
11. Find a solution of the partial different equation  $u_{xx} - u = 0$ .
12. Write the iteration formula for the Picards methods.

(12 × ¼ = 3 weights)

## Unit II

Answer any nine questions.

13. Apply  $(D + 5)^2$  to  $\sin 5x + 5x$ .
14. Find the general solution of  $y'' + 10y' + 25 = 0$ .
15. Find two linearly independent solutions of  $x^2 y'' - 2.5x y' - 2 = 0$ .
16. Find a particular solution of  $y'' - 5y' + 6y = e^x$ .
17. Reduce to first order and solve  $2xy'' = 3y'$ .
18. Find the Laplace transform of  $(t + 1)^2 e^t$ .
19. If  $L[f(x)] = F(s)$  prove that

$$L\left(\frac{f(x)}{x}\right) = \int_s^\infty F(p) dp.$$

20. Find  $L^{-1}\left[\frac{1}{s(1+2s)}\right]$ .
21. Show that  $u = x^2 + y^2$ ,  $f = 4$  satisfies the Poissons equation.
22. Find the solutions of  $u_{xx} + u_{yy} = 0$  by separating the variables.

23. Find  $a_0$  in the Fourier series expansion of  $f(x) = \begin{cases} 0 & \text{if } -2 < x < -1 \\ k & \text{if } -1 < x < 1. \\ 0 & \text{if } 1 < x < 2 \end{cases}$

24. Find first two approximate solutions  $y_1(x)$  and  $y_2(x)$  of the initial value problem  $y' = x + y$ ,  $y(0) = -1$  using Picard's method.

(9 × 1 = 9 weightage)

## Unit III

Answer any five questions.

25. Solve the initial value problem  $y'' + 1.5y' - y = 12x^2 - 6x^3 - x^4$ ,  $y(0) = 4$ ,  $y'(0) = 8$ .
26. Using method of variation of parameters solve  $y'' + y = \sec x$ .
27. Find  $t * e^t$  where  $*$  denotes convolution.

28. Using method of partial fractions find  $L^{-1}\left[\frac{s^2 + 9s - 9}{s^3 - 9s}\right]$ .

29. Using convolution find the inverse Laplace transform of  $\frac{1}{s(s^2 + 4)}$ .
30. Solve the integral equation  $y(t) = t + \int_0^t y(\tau) \sin(t - \tau) d\tau$ .
31. Find the Fourier series expansion of  $f(x) = x^2$ ,  $-\pi < x < \pi$ .
32. Using Simpson's rule with  $n = 4$  estimate  $\int_0^1 5x^4 dx$ .

(5 × 2 = 10 weightage)

**Unit IV***Answer any two questions.*

33. Solve  $x^2 y'' - 4xy' + 6y = 21x^{-4}$ .
34. Using Runge-Kutta method solve the initial value problem  
 $y' = x + y$ ,  $y(0) = 0$ ,  $h = 0.2$ .
35. Find the Fourier series of  $f(x) = \begin{cases} \frac{1}{2}(\pi + x), & -\pi \leq x < 0 \\ \frac{1}{2}(\pi - x), & 0 \leq x < \pi \end{cases}$

(2 × 4 = 8 weightage)